

verifique A del 7/9/2016

①

1) ① $(4u^4 - 2u^3 + 3u + 2) : (2u^2 + 1)$

$$\begin{array}{r|l} 4u^4 - 2u^3 + 0 + 3u + 2 & 2u^2 + 1 \\ \hline -4u^4 & 2u^2 - \frac{1}{2}u - 1 \\ \hline // & -2u^3 - 2u^2 + 3u \\ & + 2u^3 & + u \\ \hline // & -2u^2 + 4u + 2 \\ & 2u^2 & + 1 \\ \hline // & 4u + 3 \end{array}$$

Q: $2u^2 - u - 1$

R: $4u + 3$

Prove

$$(2u^2 - u - 1)(2u^2 + 1) + 4u + 3 = \cancel{4u^4} + \cancel{2u^2} - \cancel{2u^3} - \cancel{u} - \cancel{2u^2} - 1 + 4u + 3 =$$

$$= 4u^4 - 2u^3 + 3u + 2 \quad \underline{\text{OK}}$$

1) B $(b^4 - 2b^3 - 3b - 1) : (b-1)$

②

1	1	-2	0	-3	-1
1	1	-1	-1	-1	-4
1	-1	-1	-4	-4	-5
b^3	b^2	b^1	b^0		

Q: $b^3 - b^2 - b - 4$

R: -5

Prove

$$(b^3 - b^2 - b - 4)(b-1) - 5 = b^4 - b^3 - b^3 + b^2 + b^2 - b + b - 4 + 4 - 5 = b^4 - 2b^3 + 3b - 1$$

OK

2) (A)

$$(2t^3 + t^2 - 1) : (2t^2 - \frac{1}{3})$$

(3)

$2t^3$	$+t^2$	$+0$	-1	$2t^2 - \frac{1}{3}$
$-2t^3$		$+\frac{1}{3}t$		$t + \frac{1}{2}$
$=$ t^2 $\frac{1}{3}t$ -1				
	$-t^2$		$+\frac{1}{6}$	
$=$ $\frac{1}{3}t$ $-\frac{5}{6}$				

Q: $t + \frac{1}{2}$

R: $\frac{1}{3}t - \frac{5}{6}$

Prove.

$$\begin{aligned} (2t^2 - \frac{1}{3})(t + \frac{1}{2}) + \frac{1}{3}t - \frac{5}{6} &= 2t^3 + t^2 - \frac{1}{3}t - \frac{1}{6} + \frac{1}{3}t - \frac{5}{6} = \\ &= 2t^3 + t^2 - 1 \end{aligned}$$

OK

2) (B)

$$(y^4 + 2y - 1) : (y - \frac{1}{2}) =$$

(4)

1	0	0	2	-1
$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{4}$	$\frac{1}{8}$	$\frac{17}{16}$
1	$\frac{1}{2}$	$\frac{1}{4}$	$\frac{17}{8}$	$\frac{1}{16}$

$$Q : y^3 + \frac{1}{2}y^2 + \frac{1}{4}y + \frac{17}{8}$$

$$R \quad \frac{1}{16}$$

Prove

$$\begin{aligned} (y^3 + \frac{1}{2}y^2 + \frac{1}{4}y + \frac{17}{8}) (y - \frac{1}{2}) &= y^4 - \frac{1}{2}y^3 + \frac{1}{2}y^3 - \frac{1}{4}y^2 + \frac{1}{4}y^2 - \frac{1}{8}y + \frac{17}{8}y - \frac{17}{16} \\ &= y^4 + 2y - \frac{17}{16} \end{aligned}$$

OK

3) Scomponi $x^4 - 5x^3 + 2x^2 + 20x - 24$

(5)

Divisori $\pm 1 \pm 2 \pm 3 \pm 4 \pm 6 \pm 8 \pm 12 \pm 24$

Prova 1

$$1 - 5 + 2 + 20 - 24 \neq 0$$

Prova -1

$$1 + 5 + 2 - 20 - 24 \neq 0$$

Prova 2

$$16 - 40 + 8 + 40 - 24 = \underline{\underline{0}} \quad \text{~~Es~~}$$

Diviso per $\boxed{(x-2)!}$ primo fattore

1	-5	2	20	-24
2	2	-6	-8	24
1	-3	-4	12	//

$$x^3 - 3x^2 - 4x + 12$$

Prova ~~non~~ ancora con 2

$$8 - 12 - 8 + 12 = \underline{\underline{0}}$$

Diviso per $\boxed{(x-2)}$ secondo fattore

⑥

$$\begin{array}{c|ccc|c} & 1 & -3 & -6 & 12 \\ 2 & & 2 & -2 & -12 \\ \hline & 1 & -1 & -6 & // \end{array}$$

$$x^2 - x - 6 = (x-3)(x+2) \quad \left(\begin{array}{l} \text{trinomio} \\ \text{notabile} \end{array} \right)$$

$$x^4 - 5x^3 + 2x^2 + 20x - 24 = (x-2)^2 (x-3)(x+2)$$

④ Tipologia ①

$$\frac{\frac{3x+1}{x^2-4} + \frac{2}{2-x}}{\frac{3}{4-x^2}} = 2$$

$$\frac{\frac{3x+1}{(x+2)(x-2)} - \frac{2}{x-2}}{3} = 2$$

$$\frac{\cancel{(x+2)}(1)}{(2-x)(2+x)}$$

(7)

$$\frac{3x+1-2(x+2)}{(x+2)(x-2)}$$

$$= 2$$

$$- \frac{3}{(x+2)(x-2)}$$

$$\text{C.E. } x+2 \neq 0 \quad x \neq -2$$

$$x-2 \neq 0 \quad x \neq 2$$

$$\frac{3x+1-2x-4}{(x+2)(x-2)} \cdot \frac{\cancel{(x+2)}\cancel{(x-2)}}{-3} = 2$$

$$\cancel{3x} \cdot \frac{x-3}{-3} = +2 \cdot (-3)$$

$$x-3 = -6$$

$$\boxed{x = -3} \quad \text{A ce.}$$

(4) Tipologia 2

765

$$\frac{1 - \frac{x^2}{x^2+5x+6}}{1 - \frac{x^2}{x^2+x-6}} = 5$$

$$\frac{1 - \frac{x^2}{(x+2)(x+3)}}{1 - \frac{x^2}{(x+3)(x-2)}} = 5$$

C.F.
(x+2) ≠ 0 x ≠ -2
(x+3) ≠ 0 x ≠ -3

$$\frac{(x+2)(x+3) - x^2}{(x+2)(x+3)} \cdot \frac{(x+3)(x-2)}{(x+3)(x-2) - x^2} = 5$$

$$\frac{\cancel{x^2} + 5x + 6 - \cancel{x^2}}{x+2} \cdot \frac{(x-2)}{\cancel{x^2} + x - 6 - \cancel{x^2}} = 5$$

$$\frac{(5x+6)(x-2)}{(x+2)(x-6)} = 5$$

C.F. x-6 ≠ 0
x ≠ 6

$$\frac{(5x+6)(x-2)}{(x+2)(x-6)} = \frac{5(x+2)(x-6)}{(x+2)(x-6)}$$

$$5x^2 - 10x + 6x - 12 = 5(x^2 - 6x + 2x - 12)$$

$$\cancel{5x^2} - 4x - 12 = \cancel{5x^2} - 20x - 60$$

$$-4x + 20x = -60 + 12$$

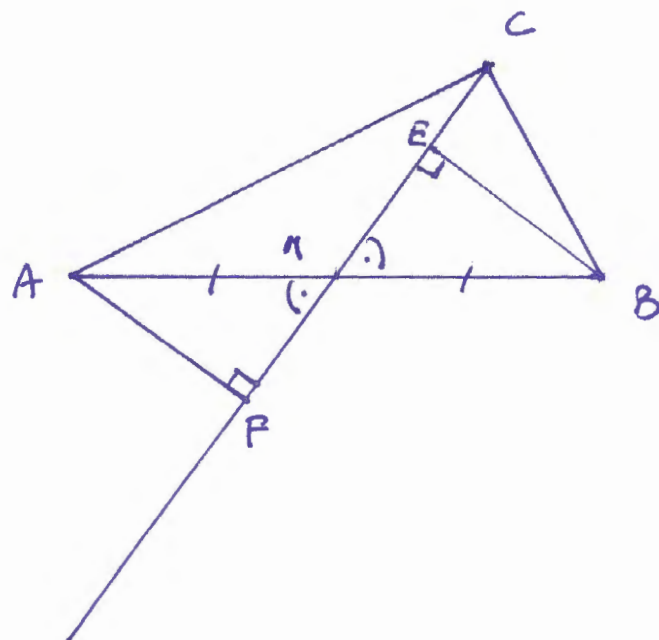
$$\frac{16x}{16} = \frac{-48}{16}$$

$$x = -3$$

NON ACC.

5)

8



$$\begin{aligned} \text{Ip: } & \overline{AM} \cong \overline{BM} \\ & \overline{BE} \perp \overline{CM} \\ & \overline{AF} \perp \overline{CM} \end{aligned}$$

$$\text{Ten: } \overline{AF} \cong \overline{BE}$$

$$1) \hat{A}MF \cong \hat{E}MB - \text{Opposti al vertice}$$

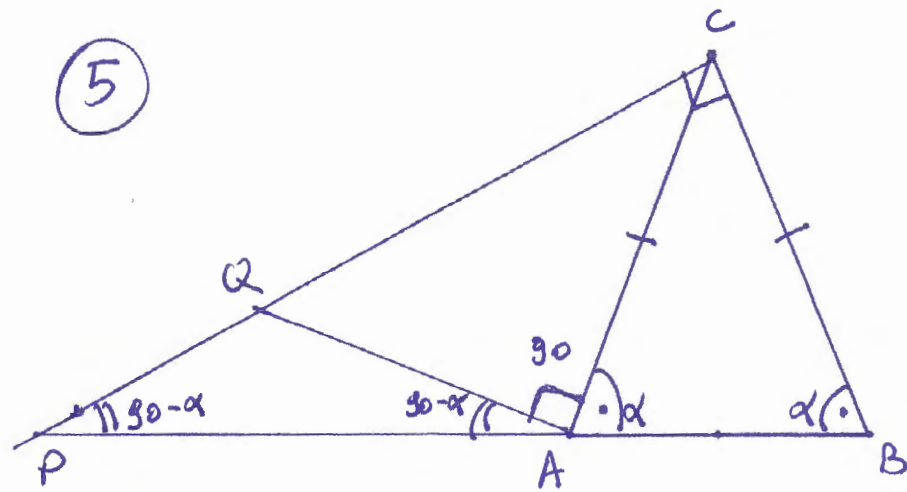
$$2) \hat{A}MF \cong \hat{B}ME - \text{II in criteriis esteso:}$$

$$\begin{aligned} & AM \cong MB (\text{Ip.}); \hat{A}MF \cong \hat{E}MB \quad (1) \\ & \hat{A}MF \cong \hat{E}MB \cong \frac{\text{II}}{2} (\text{Ip}) \end{aligned}$$

$$3) \overline{AF} \cong \overline{BE} - (2) \quad \text{Q. E. D.}$$

5

9



$$\text{I.P.: } \overline{AC} \cong \overline{BC}$$

$$\widehat{PCB} = \frac{\pi}{2}$$

$$\widehat{CAQ} = \frac{\pi}{2}$$

$$\text{Tesi: } \overline{AQ} \cong \overline{PQ}$$

$$1) \widehat{CAB} \cong \widehat{CBA} - \text{ABC isoscele.}$$

$$2) \widehat{CBP} + \widehat{CPB} = \frac{\pi}{2} - \text{Proprietà triangolo rettangolo}$$

$$3) \widehat{CAB} + \widehat{QAP} = \pi - \widehat{CAQ} = \frac{\pi}{2} - \widehat{CAQ} = \frac{\pi}{2} \text{ per I.P.}$$

$$4) \widehat{QPA} \cong \widehat{QAP} - \text{complementari angoli complementari (1), (2), (3)}$$

$$5) \overline{AQ} \cong \overline{PQ} - \text{proprietà triangoli isosceli (4)}$$

Q.E.D.



$$AB = 2BC + 5$$

$$\frac{3AB - BC}{2AB + BC} = \frac{4}{3}$$

$$BC = x \Rightarrow AB = 2 \cdot x + 5$$

$$\frac{3(2x+5) - x}{2(2x+5) + x} = \frac{4}{3}$$

$$\frac{6x+15-x}{4x+10+x} = \frac{4}{3}$$

$$\frac{5x+15}{5x+10} = \frac{4}{3}$$

$$\frac{5x+15}{5(x+2)} - \frac{4}{3} = 0$$

$$\frac{3(5x+15) - 20(x+2)}{15(x+2)} = 0$$

C.E. $x \neq -2$
(x é sempre positivo)

$$15x + 45 - 20x - 40 = 0$$

$$15x + 45 - 20x - 40 = 0$$

$$-5x + 5 = 0$$

$$5x = 5 \quad \boxed{x = 1}$$

$$ACE \Rightarrow \begin{matrix} BC = 1 \\ AB = 7 \end{matrix}$$

$$2P = 2 \cdot (7+1) = \underline{16}$$

Verify B

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1) (A) $(9y^4 - 6y^3 - 3y - 2) : (2 - 3y^2)$

$$\begin{array}{r|l} 9y^4 - 6y^3 + 0 - 3y - 2 & -3y^2 + 2 \\ -9y^4 & -3y^2 + 2y - 2 \\ \hline // -6y^3 + 6y^2 - 3y & \\ + 6y^3 & \\ \hline // 6y^2 - 7y - 2 & \\ -6y^2 & + 4 \\ \hline // -7y + 2 & \end{array}$$

Q: $-3y^2 + 2y - 2$ R: $-7y + 2$

prove

$$\begin{aligned} & (-3y^2 + 2y - 2) \cdot (2 - 3y^2) - 7y + 2 = \\ & -\cancel{6y^2} + 9y^4 + 4y - 6y^3 - 4 + \cancel{6y^2} - 7y + 2 = \\ & = 9y^4 - 6y^3 - 3y - 2 \quad \underline{\text{OK}} \end{aligned}$$

1) (B) $(y^4 + y - 4) : (y + 2)$

	1	0	0	1	-4
-2		-2	4	-8	+14
	1	-2	4	-7	+10 +10
	y^3	y^2	y		

$Q: y^3 - 2y^2 + 4y - 7$ $R: \cancel{-18} + 10$

Prove

$$\begin{aligned}
 & (y^3 - 2y^2 + 4y - 7) \cdot (y + 2) + 10 = \\
 & = y^4 + \cancel{2y^3} - \cancel{2y^3} - \cancel{4y^2} + \cancel{4y^2} + 8y - 7y - 14 + 10 = \\
 & = y^4 + y - 4 \quad \underline{\underline{OK}}
 \end{aligned}$$

2) (A)

(13)

$$(b^4 - 2b^3 - 3b - 1) : (2b^2 - \frac{1}{2})$$

$ \begin{array}{r} b^4 - 2b^3 \quad 0 \quad -3b - 1 \\ -b^4 \quad 0 \quad +\frac{1}{4}b^2 \\ \hline // \quad -2b^3 \quad \frac{1}{4}b^2 \quad -3b \\ \quad 2b^3 \quad \quad -\frac{1}{2}b \\ \hline // \quad \quad \frac{1}{4}b^2 \quad -\frac{7}{2}b - 1 \\ \quad \quad -\frac{1}{4}b^2 \quad \quad +\frac{1}{16} \\ \hline // \quad \quad \quad -\frac{7}{2}b - \frac{15}{16} \end{array} $	$ \begin{array}{r} 2b^2 - \frac{1}{2} \\ \hline \frac{1}{2}b^2 - b + \frac{1}{8} \end{array} $
--	--

$$Q = \frac{1}{2}b^2 - b + \frac{1}{8}$$

$$R = -\frac{7}{2}b - \frac{15}{16}$$

prove : $(\frac{1}{2}b^2 - b + \frac{1}{8})(2b^2 - \frac{1}{2}) - \frac{7}{2}b - \frac{15}{16} =$

$$= b^4 - \cancel{\frac{1}{2}b^2} - 2b^3 + \frac{1}{2}b + \cancel{\frac{1}{4}b^2} - \frac{1}{16} - \frac{7}{2}b - \frac{15}{16} =$$

$$\underline{b^4 - 2b^3 - 3b - 1} \quad \text{OK}$$

2) (B)

$$(u^5 - 2u^3 + u + 1) : (u - \frac{1}{2})$$

(14)

1	0	-2	0	1	1
$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{4}$	$-\frac{7}{8}$	$-\frac{7}{16}$	$\frac{9}{32}$
1	$\frac{1}{2}$	$-\frac{7}{4}$	$-\frac{7}{8}$	$\frac{9}{16}$	$\frac{41}{32}$
u^4	u^3	u^2	u		

$$Q: u^4 + \frac{1}{2}u^3 - \frac{7}{4}u^2 - \frac{7}{8}u + \frac{9}{16} \quad R: \frac{41}{32}$$

PROVA : $(u^4 + \frac{1}{2}u^3 - \frac{7}{4}u^2 - \frac{7}{8}u + \frac{9}{16})(u - \frac{1}{2}) + \frac{41}{32} =$

$$= u^5 - \frac{1}{2}u^4 + \frac{1}{2}u^4 - \frac{1}{4}u^3 - \frac{7}{4}u^3 + \frac{7}{8}u^2 - \frac{7}{8}u^2 + \frac{7}{16}u + \frac{9}{16}u - \frac{9}{32} + \frac{41}{32} =$$

$$= u^5 - 2u^3 + u + 1 \quad \underline{\underline{OK}}$$

3) Scampom: $X^4 - 6X^3 + 5X^2 + 24X - 36$

(15)

Divisori di 36: $\pm 1; \pm 2; \pm 3; \pm 4; \pm 6 \dots$

Prova 1

$$1 - 6 + 5 + 24 - 36 \neq 0$$

Prova -1

$$1 + 6 + 5 - 24 - 36 \neq 0$$

Prova 2

$$16 - 6 \cdot 8 + 5 \cdot 4 + 48 - 36 = 16 - 48 + 20 + 48 - 36 = \underline{\underline{0}}$$

1	- 6	5	24	- 36
2	2	- 8	- 6	36
1	- 4	- 3	18	0

$$X^3 - 4X^2 - 3X + 18$$

$(X - 2)$ primo fattore.

Prova ancora 2

$$8 - 16 - 6 + 18 = 4 \neq 0$$

Prova -2

$$-8 - 16 + 6 + 18 = \underline{\underline{0}}$$

$$\begin{array}{ccc|c} 1 & -4 & -3 & 18 \\ -2 & & -2 & 12 \\ \hline 1 & -6 & 9 & 0 \end{array}$$

$$x^2 - 6x + 9 = (x-3)^2$$

$$\boxed{x+2}$$

keine weitere

$$x^4 - 6x^3 + 5x^2 + 24x - 36 = (x+2)(x-2)(x-3)^2$$

$$4) \left(\frac{2}{x-1} + \frac{1}{x+1} \right)^{-1} : (x+1) - \frac{3x^2}{9x^2-1} = \frac{2}{3x-1}$$

$$\left(\frac{2(x+1) + (x-1)}{(x-1)(x+1)} \right)^{-1} \cdot \frac{1}{x+1} - \frac{3x^2}{(3x+1)(3x-1)} = \frac{2}{3x-1}$$

$$\left(\frac{(x-1)\cancel{(x+1)}}{2x+2+x-1} \right) \cdot \frac{1}{\cancel{(x+1)}} - \frac{3x^2}{(3x+1)(3x-1)} = \frac{2}{3x-1}$$

C.E.
 $x-1 \neq 0 \quad x \neq 1$
 $x+1 \neq 0 \quad x \neq -1$
 $3x+1 \neq 0 \quad x \neq -\frac{1}{3}$
 $3x-1 \neq 0 \quad x \neq \frac{1}{3}$

$$\frac{x-1}{3x+1} - \frac{3x^2}{(3x+1)(3x-1)} - \frac{2}{3x-1} = 0$$

$$\frac{(x-1)(3x-1) - 3x^2 - 2(3x+1)}{(3x+1)(3x-1)} = 0$$

$$\cancel{3x} - x - 3x + 1 - \cancel{3x^2} - 6x - 2 = 0$$

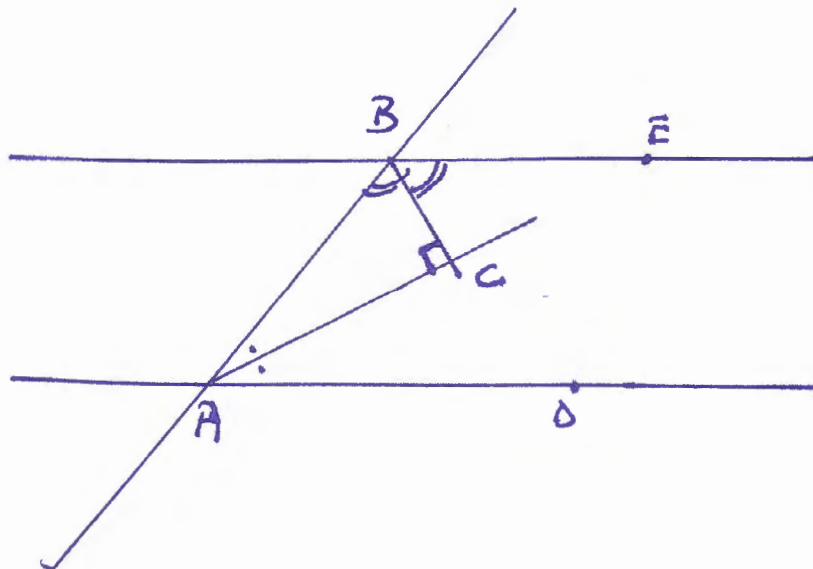
$$-10x - 1 = 0 \quad -10x = +\underline{1}$$

$$\boxed{x = -\frac{1}{10}} \text{ Acc}$$

(17)

5)

18



$$HP : BE \parallel AD$$

$$\widehat{BAC} \cong \widehat{CAD}$$

$$\widehat{ABC} \cong \widehat{EBC}$$

$$Th : ~~BC~~ \widehat{BCA} = \frac{\pi}{2}$$

$$1) \widehat{DAB} + \widehat{ABE} = \pi - \text{Complementary interior}$$

$$2) \widehat{DAB} = 2 \widehat{CAB} - \text{per I.P. CA bisectore di } \widehat{BAD}$$

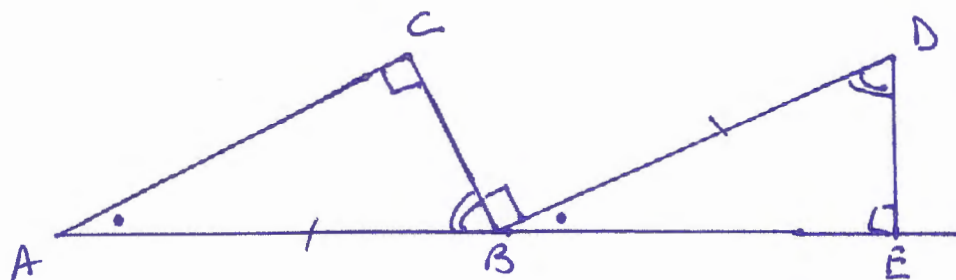
$$3) \widehat{ABE} = 2 \widehat{ABC} - \text{Per I.P. BC bisectore di } \widehat{ABE}$$

$$4) 2 \widehat{CAB} + 2 \widehat{ABC} = \pi - \text{per (1), (2) e (3)}$$

$$5) \widehat{CAB} + \widehat{ABC} = \frac{\pi}{2} - \text{per (4) . Q.E.D.}$$

6)

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$$H.P.: \overline{AC} \cong \overline{BD}$$

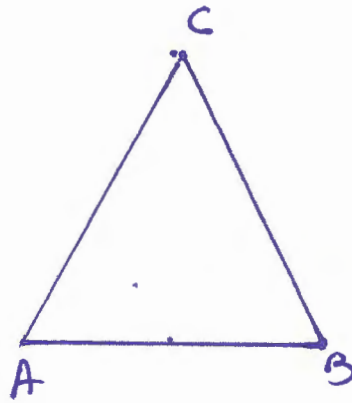
$$\widehat{ACB} \cong \widehat{CBD} \cong \widehat{BED} = \frac{\pi}{2}$$

$$Th.: \triangle ABC \cong \triangle BDE$$

- 1) $\widehat{ABC} + \widehat{CAB} = \frac{\pi}{2}$ - Angoli acuti triangolo rettangolo
- 2) $\widehat{ABC} + \widehat{CBD} + \widehat{DBE} = \pi$ - I.P.
- 3) $\widehat{ABC} + \widehat{DBE} = \frac{\pi}{2}$ - per (2) e ~~def.~~ $\widehat{CBD} = \frac{\pi}{2}$ (I.P.)
- 4) $\widehat{DBE} \cong \widehat{CAB}$ - per (1) e (3) - complementari stesso angolo
- 5) $\widehat{BDE} \cong \widehat{ABC}$ - per (1) e (4) - complementari angoli complementari
- 6) $\triangle ABC \cong \triangle BDE$ - I.criterio: $\overline{AC} \cong \overline{BD}$ (I.P.); $\widehat{CAB} \cong \widehat{DBE}$ (4); $\widehat{BDE} \cong \widehat{ABC}$ (5)

Q.E.D.

7)



$$BC = AB + 6$$

$$\frac{CB + 5AB}{2AB} = \frac{10}{3}$$

$$AB = x \Rightarrow BC = x + 6$$

$$\frac{x + 6 + 5x}{2x} = \frac{10}{3}$$

$$\frac{3(6x + 6)}{6x} = \frac{20x}{6x}$$

$$\begin{array}{l} \text{C.E} \\ x \neq 0 \end{array}$$

$$18x + 18 = 20x$$

$$2x = 18$$

$$\boxed{x = 9}$$

$$AB = 9$$

$$BC = 15$$

$$2p = 9 + 15 \cdot 2 = \boxed{39 \text{ cm}}$$

verify C

(21)

1) A $(u^5 - 2u^3 + u + 1) : (u^2 + u + 1)$

u^5	0	$-2u^3$	0	u	1	$u^2 + u + 1$
$-u^5$	$-u^4$	$-u^3$				$u^3 - u^2 - 2u + 3$
$//$	$-u^4$	$-3u^3$	0			
	u^4	$+u^3$	$+u^2$			
$=$		$-2u^3$	u^2	u		
		$2u^3$	$2u^2$	$2u$		
	$//$		$3u^2$	$3u$	1	
			$-3u^2$	$-3u$	-3	
		$//$		$=$	-2	

Q: $u^3 - u^2 - 2u + 3$ R: -2

Prove:

$$\begin{aligned}
 & (u^3 - u^2 - 2u + 3)(u^2 + u + 1) - 2 = \\
 & = u^5 + \cancel{u^4} + \cancel{u^3} - \cancel{u^4} - \cancel{u^3} - \cancel{u^2} - 2u^3 - \cancel{2u^2} - 2u + 3\cancel{u^2} + 3\cancel{u} + 3 - 2 = \\
 & = u^5 - 2u^3 + u + 1 \quad \underline{\text{OK}}
 \end{aligned}$$

1) B

(22)

$$(a^4 - 3a^3 - 1) : (a - 3)$$

1	- 3	0	0	- 1
3	3	0	0	0
1	0	0	0	- 1

$$Q = a^3$$

$$R = -1$$

prove

$$(a^3)(a - 3) - 1 = a^4 - 3a^3 - 1 \quad \underline{\text{OK}}$$

2) A

$$(t^4 + t - 4) : (2t^2 + \frac{1}{2})$$

(23)

t^4	0	0	t	-4	$2t^2 + \frac{1}{2}$
$-t^4$		$-\frac{1}{4}t^2$			$\frac{1}{2}t^2 - \frac{1}{8}$
// $-\frac{1}{4}t^2$ t -4					
		$\frac{1}{4}t^2$		$+\frac{1}{16}$	
		$=$		$t - \frac{63}{16}$	

$$Q: \frac{1}{2}t^2 - \frac{1}{8}$$

$$R: t - \frac{63}{16}$$

Prüfung

$$\begin{aligned}
 & \left(\frac{1}{2}t^2 - \frac{1}{8}\right) \left(2t^2 + \frac{1}{2}\right) + t - \frac{63}{16} = \\
 & = t^4 + \cancel{\frac{1}{4}t^2} - \cancel{\frac{1}{4}t^2} - \frac{1}{16} + t - \frac{63}{16} = t^4 + t - 4 \quad \underline{\underline{OK}}
 \end{aligned}$$

2) B

$$(9y^4 - 6y^3 - 3y - 2) : (y - \frac{1}{3})$$

(29)

	9	- 6	0	- 3	- 2
$\frac{1}{3}$		3	- 1	$-\frac{1}{3}$	$-\frac{10}{9}$
	9	- 3	- 1	$-\frac{10}{3}$	$-\frac{28}{9}$
	y^3	y^2	y		

$$Q: 9y^3 - 3y^2 - y - \frac{10}{3}$$

$$R: -\frac{28}{9}$$

$$\text{Proof: } (9y^3 - 3y^2 - y - \frac{10}{3}) \cdot (y - \frac{1}{3}) - \frac{28}{9} =$$

$$9y^4 - 3y^3 - 3y^3 + \cancel{y^2} - \cancel{y^2} + \frac{1}{3}y - \frac{10}{3}y + \frac{10}{9} - \frac{28}{9} =$$

$$9y^4 - 6y^3 - \frac{3}{3}y - 2 \quad \underline{\underline{OK}}$$

3) scomponi: ~~$x^4 - 8x^3$~~

(25)

$$x^4 - x^3 - 10x^2 + 4x + 24$$

divisori di 24: $\pm 1; \pm 2; \pm 3; \pm 4; \pm 6; \dots$

prova 1

$$1 - 1 - 10 + 4 + 24 \neq 0$$

prova -1

$$1 + 1 - 10 - 4 + 24 \neq 0$$

prova 2

$$16 - 8 - 40 + 8 + 24 = \underline{\underline{0}}$$

	1	-1	-10	4	24
2	1	2	2	-16	-24
	1	1	-8	-12	0

$x - 2$ primo fattore

$$x^3 + x^2 - 8x - 12$$

prova ancora 2

$$8 + 4 - 16 - 12 \neq 0$$

prova -2

26

$$-8 + 4 + 16 - 12 = 0$$

	1	1	-8	-12
-2		-2	2	12
	1	-1	-6	0

$$x^2 - x - 6$$

$(x+2)$ secondo fattore

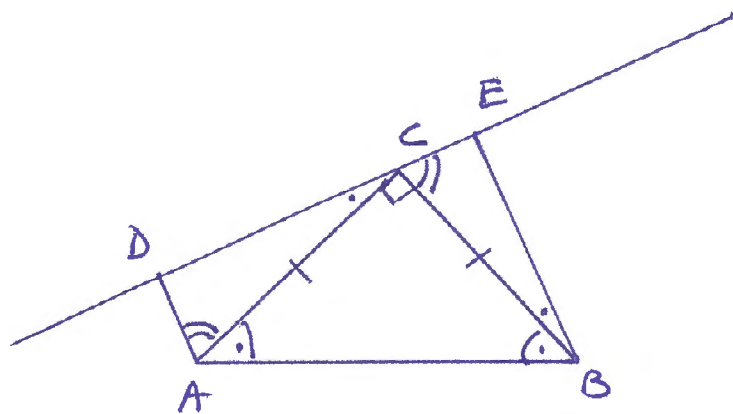
$$x^2 - x - 6 = (x-3)(x+2) \quad \text{troviamo un altro}$$

$$x^4 - x^3 - 10x^2 + 9x + 24 = (x-2)(x+2)^2(x-3)$$

4) Volei pag. 6

5)

(27)



H/p: $\overline{CA} \cong \overline{CB}$

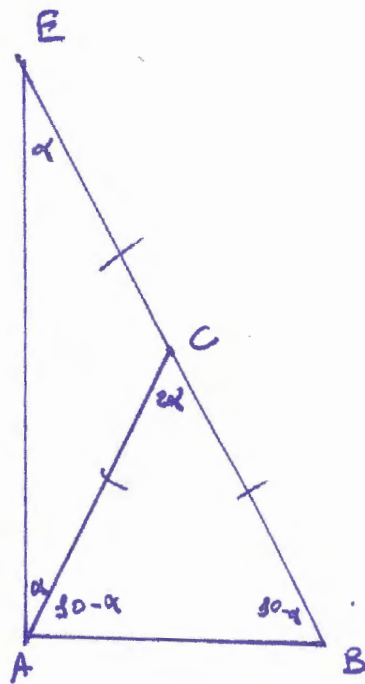
$$\angle ACB \cong \angle ACD \cong \angle ECB = \frac{\pi}{2}$$

Th $\overline{DE} = \overline{AD} + \overline{BE}$

- 1) $\angle DCA + \angle ACB + \angle BCE = \pi$ - per I.p.
- 2) $\angle ABC + \angle BCA + \angle CAB = \pi$ - somma angoli interni $\triangle ABC$
- 3) $\angle DCA + \angle ECB = \boxed{\pi} - \angle ACB = \frac{\pi}{2}$ - per (2)
- 4) $\angle DCA \cong \angle ECB$ - complementari stesso angolo
- 5) $\angle DAC \cong \angle EBC$ - complementari stesso angolo
- 6) $\triangle DAC \cong \triangle ECB$ - II criterio: $AC \cong BC$ (I.p.), (4), (5)
- 7) $\overline{DA} \cong \overline{CE}; \overline{DC} \cong \overline{EB}$ - (6)
- 8) $\overline{DE} \cong \overline{DC} + \overline{CE} \cong \overline{EB} + \overline{DA}$ Q.E.D.

6)

(28)



$$HP \quad AC \cong BC \cong CE$$

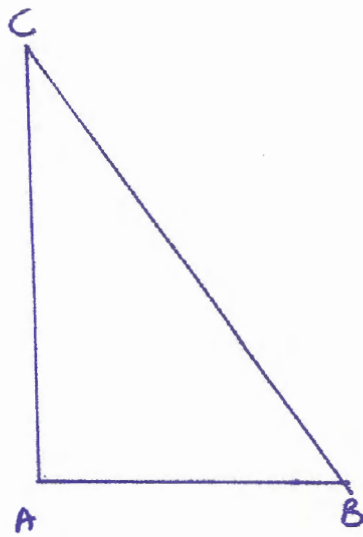
$$TH \quad \widehat{EAB} = \frac{\pi}{2}$$

- 1) $\widehat{ACB} = \widehat{AEC} + \widehat{EAC}$ - Angolo esterno
- 2) $\widehat{ACB} = 2 \widehat{EAC}$ - (1) e proprietà triangoli isosceli
- 3) $\widehat{ACB} + \widehat{CAB} + \widehat{CBA} = \pi$ - Angoli interni triangolo
- 4) $2 \widehat{EAC} + 2 \widehat{CAB} = \pi$ - per (2) e proprietà triangoli isosceli
- 5) $\widehat{EAC} + \widehat{CAB} = \frac{\pi}{2}$ per 4
- 6) $\widehat{EAB} = \frac{\pi}{2}$ per 5

Q. E. D.

7)

(29)



$$AB = \frac{2}{3} AC + 1$$

$$\frac{AB + 2AC}{3AC - AB} = \frac{11}{9}$$

$$AC = x \quad AB = \frac{2}{3}x + 1$$

$$\frac{\frac{2}{3}x + 1 + 2x}{3x - \left(\frac{2}{3}x + 1\right)} = \frac{11}{9}$$

$$\frac{\frac{2x + 3 + 6x}{3}}{\frac{8x - 2x - 3}{3}} = \frac{11}{9}$$

$$\text{C.E. } x \neq \frac{3}{7}$$

$$\frac{2x + 3 + 6x}{7x - 3} = \frac{11}{9}$$

$$\frac{8x + 3}{7x - 3} \cdot \frac{11}{9} = 0$$

$$\frac{9(8x + 3) - 11(7x - 3)}{9(7x - 3)} = 0$$

$$72x + 27 - 77x + 33 = 0$$

$$-5x = 60 \quad x = 12$$

$$AC = 12$$

$$AB = \frac{2}{3} \cdot 12 + 1 = 9$$

$$BC = \sqrt{144 + 81} = \sqrt{225} = 15$$

$$\text{LP} = 12 + 9 + 15 = 36 \text{ cm}$$